

Formal Verification of Floating-Point Hardware with Assertion-Based VIP

Ravi Ram, Adam Elkins, Adnan Pratama – Xilinx Inc.

Sasa Stamenkovic, Sven Beyer, Sergio Marchese – OneSpin Solutions







- Floating-point (FP) arithmetic
- Functional verification of FP hardware
- Formal verification with assertion-based VIP
- Results
- Conclusions



Floating-Point Arithmetic

- Compared to fixed-point arithmetic
 - Covers wider range of values
 - No loss of precision, higher accuracy
 - More complex hardware
 - Notoriously hard to verify



IEEE 754 Half / Single / Double / ... Precision



Functional Verification

- Simulation misses bugs
 - Exhaustive verification is not feasible
 - One and a half engineer-years to cover all scenarios
 - Many implementation-dependent corner cases
- Sequential Equivalence Checking (SEC) of RTL against reference model
 - Requires detailed understanding of both implementations
 - Reference model (C++/SystemC) needs adaptation
 - High effort, little reusability
- Formal Assertion-Based VIP (ABVIP
 - Xilinx tried but ran into usability and convergence issues
 - Xilinx worked with OneSpin to develop a new solution







Floating-Point ABVIP

FP ABVIP

- SystemVerilog package
- *ieee_...* functions and data types
- No reference model required
- Minimal design knowledge by end user

OneSpin Tool

- FP ABVIP available
- Proof engines/strategies for arithmetic
- Debug with FP data types





Floating-Point ABVIP

- Compliant to IEEE-754
- Supports
 - Half, single and double precision formats
 - All the rounding modes and the exception flags
 - Tininess before or after rounding
 - Add, sub, mult, absolute value, negation, and all comparison operations
 - Conversion functions also included
- Customizable
 - Custom precision
 - Intended deviations from standard







- Supports addition, subtraction and multiplication
- Tool found a previously undiscovered bug in the module interface constraints
- General and specific scenarios assertions created
 - e.g. operations with signalling or quiet NaN
- Design bugs previously found in simulation and emulation
 FP ABVIP found them within seconds





• Open Cores

Operation	# bugs	Setup effort	Runtime	Result
FADD	0	30 minutes	52 seconds	Full proof
FSUB	1	5 minutes	1 minute to find a bug	Fail
FMUL	2	5 minutes	1 second to find a bug	Fail

• Xilinx FPU

Operation	# bugs	Setup effort	Runtime	Result
FADD	0	4 days	3 minutes	Full proof
FSUB	0	3 days	1 minute	Full proof
FMUL	1	15 days	4 minutes	Full proof

Tool and FPU App familiarization and constraints setup



Formal Coverage

- Metric-driven verification
 - OneSpin Quantify
- Answers
 - How much has been verified?
 - What is the next assertion to write?
 - Is my design over-constrained?
- User written assertions and covers
- Overall coverage ~90%
- Holes point to logic not contributing floating-point operations





Formal coverage results

				Verif	ied with asse	rtions
Struct	ural Coverage Overview	1				
Status		Statements	e		Branches	5
1	covered	185		99.46%	15	51.72%
R	reached	0	0.00%		0	0.00%
U	unknown	0	0.00%		2	6.90%
0R	unobserved	1	0.54%		0	0.00%
0	uncovered	0	0.00%		0	0.00%
0C	constrained	0	0.00%		0	0.00%
0D	dead	0	0.00%		12	41.38%
Sum	quantify targets	186			29	

Excluded Code Overview						
Code Status		Statements		Branches		
Xu	excluded by user	697	75.84%	286	89.38%	
Xr	excluded redundant code	36	3.92%	5	1.56%	
Xν	excluded verification code	0	0.00%	0	0.00%	
0/1/U	quantify targets	186	20.24%	29	9.06%	
Sum	total code	919		320		





- FP ABVIP is compliant with the IEEE 754 standard
- Solution is easy to set up and use
- Excellent experience for Xilinx FPU project
 - Low effort
 - Uncovered corner-case bugs within seconds
 - Exhaustive verification with full proofs, within minutes
 - High coverage
- Current limitations
 - No support for iterative operations (division, square root)
 - Additional effort may be required to achieve full proofs