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**DVCON**  
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# See the Forest for the Trees – How to Effectively Model and Randomize a DRT Structure

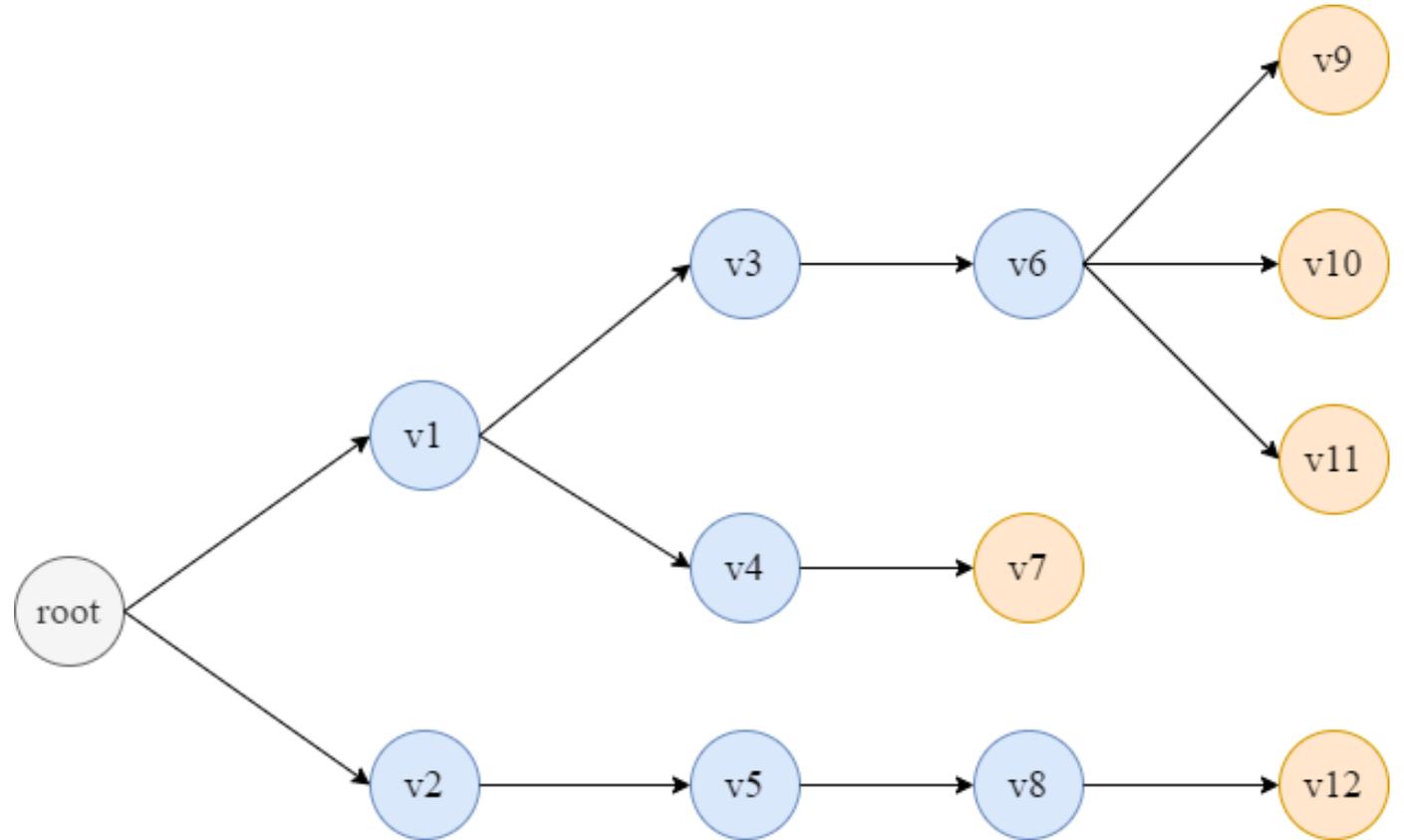
Harry Duque and Lars Viklund





# Graphs and Trees

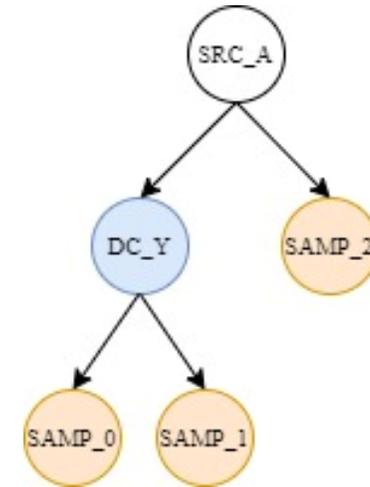
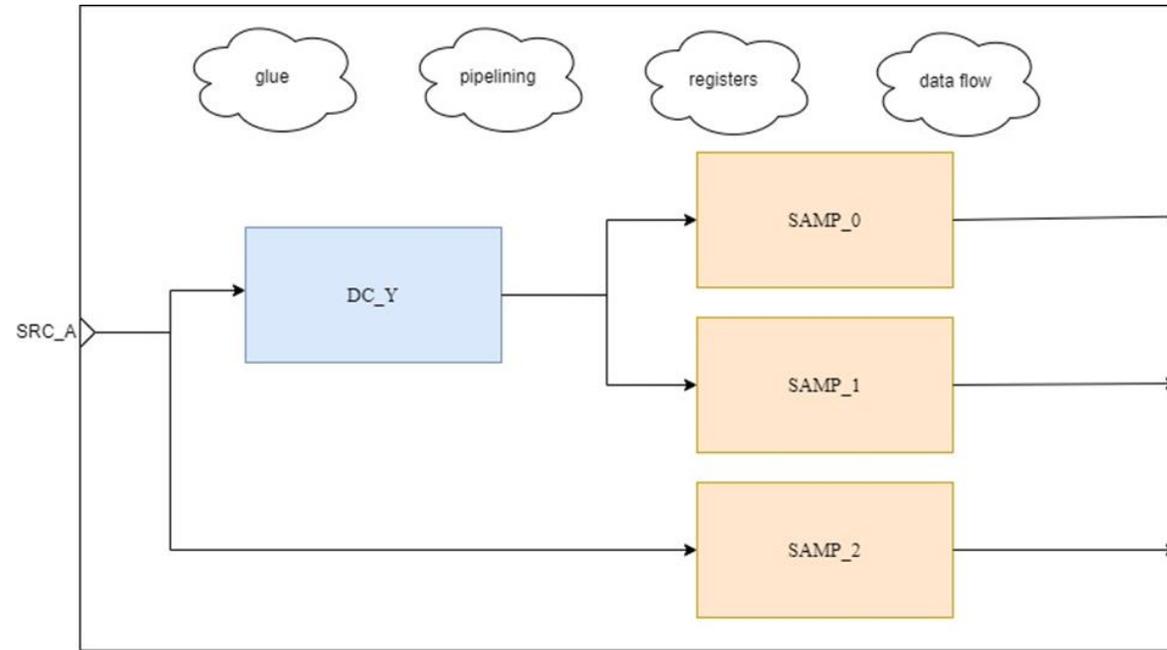
- Directed Rooted Tree (DRT)
  - Connected
  - Oriented
  - Acyclic
  - Each vertex has a single parent
  - Single start point, a root
  - All edges point away from root



# Highly Configurable Datapath Unit



# Modelling of Connectivity



# Challenges

## Validity

- Rules
- Constraints

## Controllability

- Steer
- Direct

## Performance

- Solver

## Scalability

- Vertices
- Entry

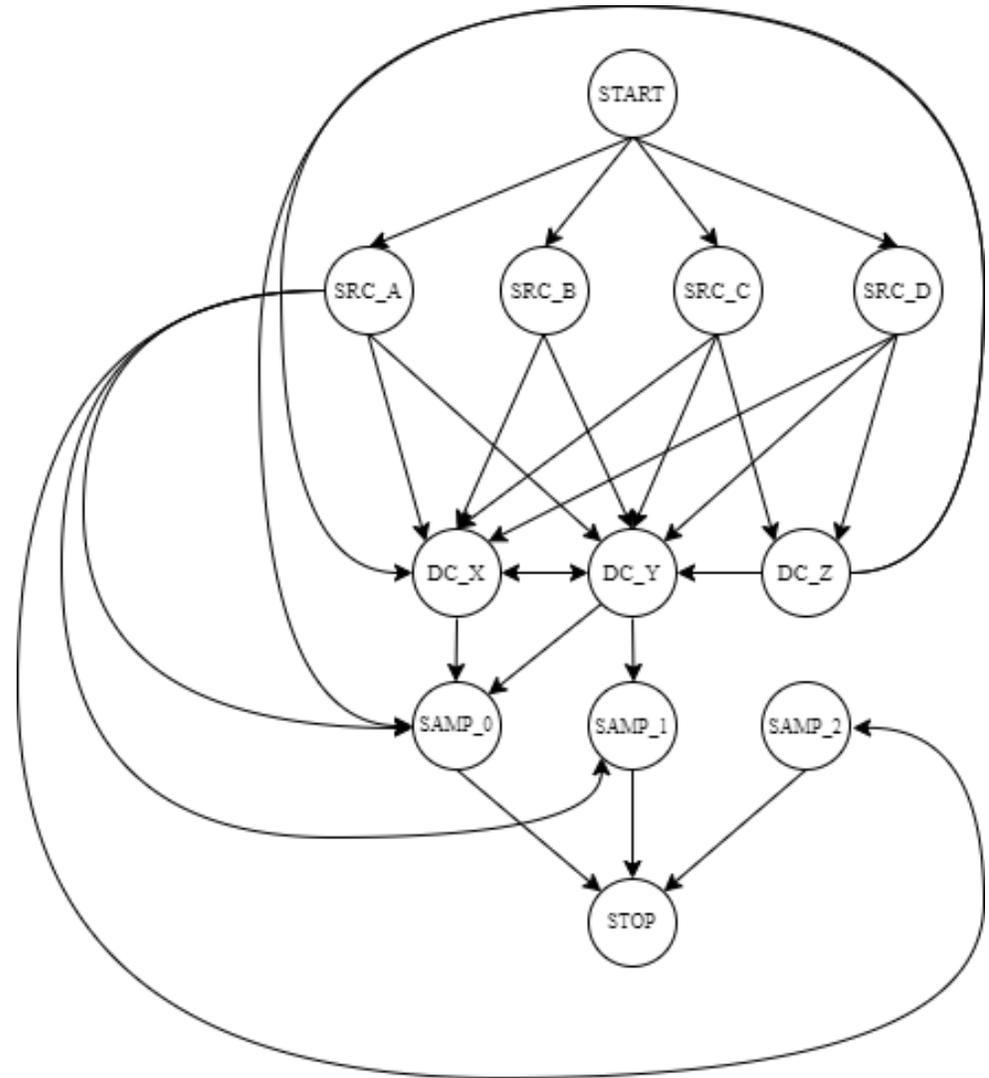


# See the Forest from the Trees

- Tree has a recursive, self-similar shape
- Recursion
- Search problem
- Backtracking

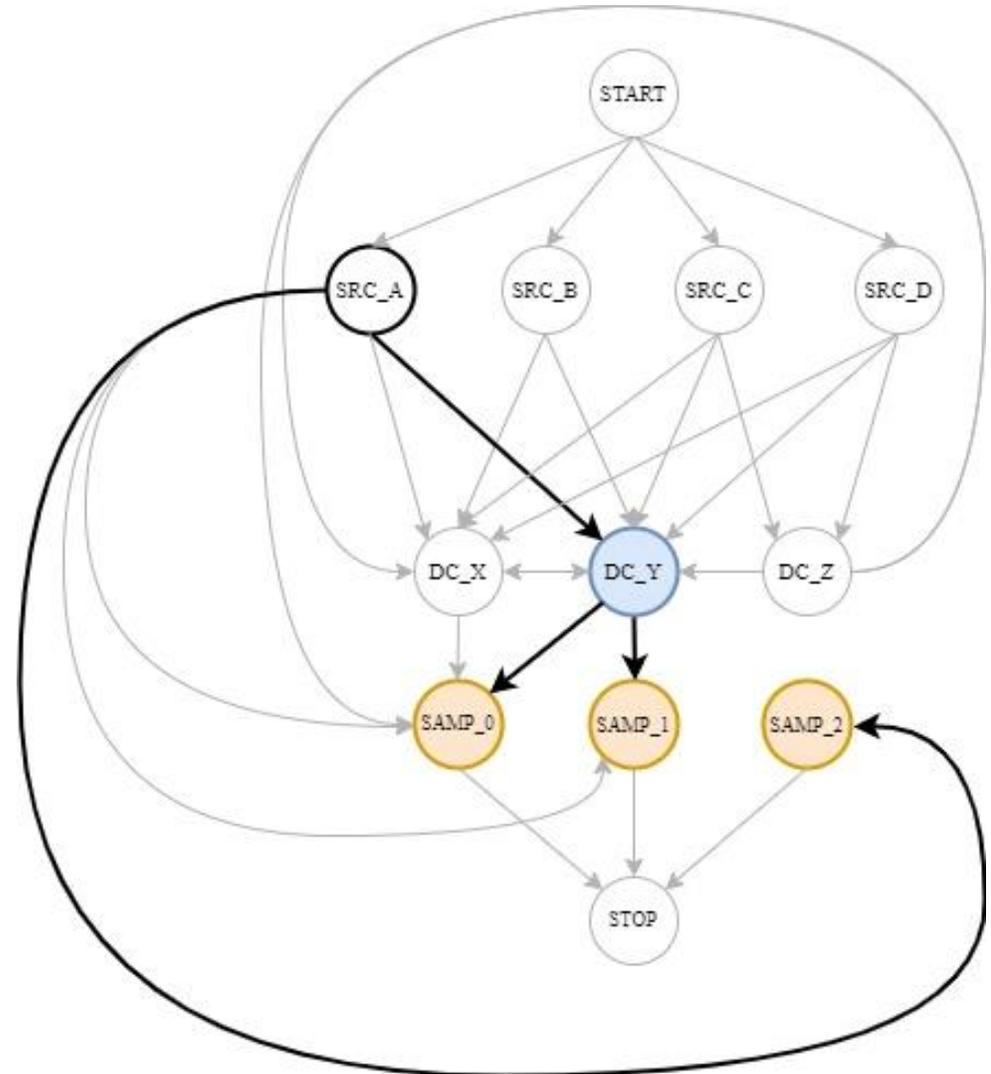
# Model of Solution Space

- SRC\_<\*>: A primary input
- DC\_<\*>: A converter sub-unit
- SAMP\_<\*>: A sampler sub-unit
- Helper START and STOP vertices



# A possible solution

- SRC\_<\*>: A primary input
- DC\_<\*>: A converter sub-unit
- SAMP\_<\*>: A sampler sub-unit
- Helper START and STOP vertices



# Model of Solution Space in Constraints

```
class vertex extends vertex_base#(id_t, config_t);
  constraint c_connectivity {
    this.id inside {START}           -> this.child_id inside {SRC_A, SRC_B, SRC_C, SRC_D};
    this.id inside {SRC_A}           -> this.child_id inside {DC_X, DC_Y, SAMP_0, SAMP_1, SAMP_2};
    this.id inside {SRC_B}           -> this.child_id inside {DC_X, DC_Y};
    this.id inside {SRC_C, SRC_D}    -> this.child_id inside {DC_X, DC_Y, DC_Z};
    this.id inside {DC_X}            -> this.child_id inside {DC_Y, SAMP_0};
    this.id inside {DC_Y}            -> this.child_id inside {DC_X, SAMP_0, SAMP_1};
    this.id inside {DC_Z}            -> this.child_id inside {DC_X, DC_Y, SAMP_0};
    this.id inside {SAMP_0,
                    SAMP_1,
                    SAMP_2}         -> this.child_id inside {STOP};
  }
}
```

# Backtracking

- Incrementally builds solution candidates
- Abandons potential candidates when not meeting criteria
- Guaranteed to produce a valid solution

```
function find(vertex v);  
    if abandon(v) prune(v)  
    if leaf(v) output(v)  
    foreach children(v)[i]  
        find(i)  
endfunction : find
```

# Building the Tree

- Separate allocator class
- Implements the different described functions for backtracking
- For implementation refer to the paper.

```
function find(vertex v);  
    if abandon(v) prune(v)  
    if leaf(v) output(v)  
    foreach children(v)[i]  
        find(i)  
endfunction : find
```

```
if (!current.randomize() with {!(this.child_id inside {local::withdrawn});}) begin
  this.withdrawn.push_front(current.id);
  return 0;
end
```

abandon(v)

prune(v)

```
if (current.child_id == stop) begin
  this.withdrawn.push_front(current.id);
  return 1;
end
```

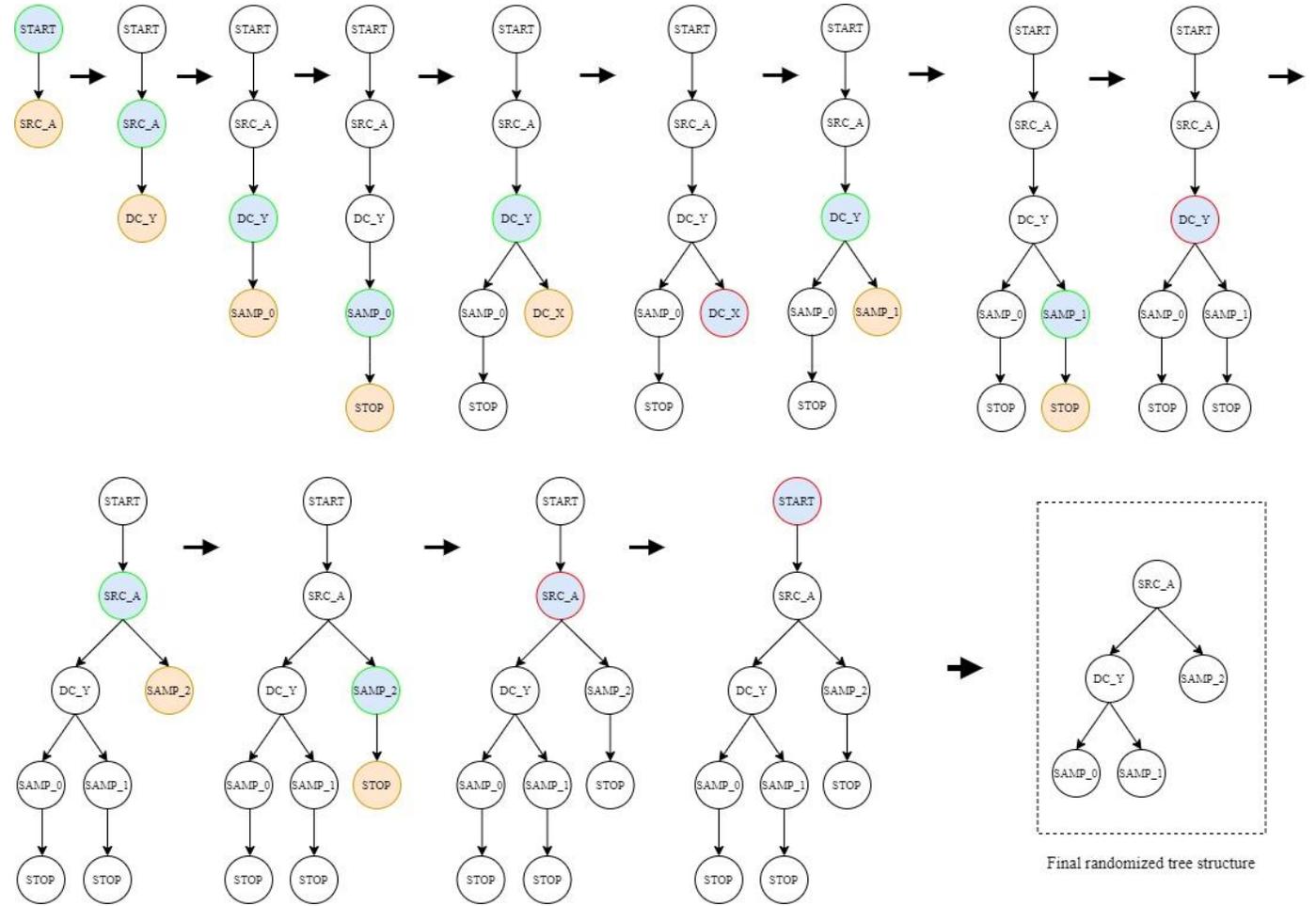
leaf(v)

output(v)

```
child = vertex_base#(id_t, config_t)::type_id::create();
child.init(current.child_id, current.id, this);
this.withdrawn.push_back(current.id);
ok = find_path(child, stop);
this.withdrawn.pop_back(current.id);
if (ok) begin
  this.withdrawn.push_front(current.id);
  current.add_child(child);
  return 1;
end
```

recursion

# An Example



# An Example



-  Vertex under randomization - Successful
-  Vertex under randomization - Failure
-  Randomized child vertex

```
withdrawn = {}
```

```
this.id inside {START}      -> this.child_id inside {SRC_A, SRC_B, SRC_C, SRC_D};
```

# An Example

-  Vertex under randomization - Successful
-  Vertex under randomization - Failure
-  Randomized child vertex



```
withdrawn = {}
```

```
this.id inside {START} -> this.child_id inside {SRC_A, SRC_B, SRC_C, SRC_D};
```

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-  Vertex under randomization - Successful
-  Vertex under randomization - Failure
-  Randomized child vertex

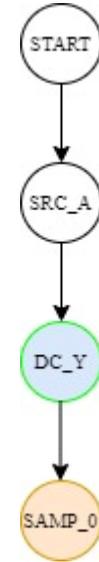


```
withdrawn = {SRC_A}
```

```
this.id inside {SRC_A} -> this.child_id inside {DC_X, DC_Y, SAMP_0, SAMP_1, SAMP_2};
```

# An Example

-  Vertex under randomization - Successful
-  Vertex under randomization - Failure
-  Randomized child vertex



```
withdrawn = {SRC_A, DC_Y}
```

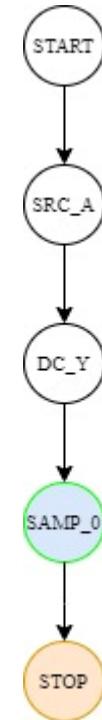
```
this.id inside {DC_Y} -> this.child_id inside {DC_X, SAMP_0, SAMP_1};
```

# An Example

-  Vertex under randomization - Successful
-  Vertex under randomization - Failure
-  Randomized child vertex

```
withdrawn = {SRC_A, DC_Y, SAMP_0}
```

```
this.id inside {SAMP_0, SAMP_1, SAMP_2} -> this.child_id inside {STOP};
```

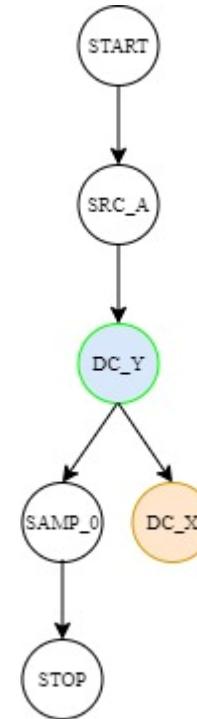


# An Example

-  Vertex under randomization - Successful
-  Vertex under randomization - Failure
-  Randomized child vertex

```
withdrawn = {SRC_A, DC_Y, SAMP_0}
```

```
this.id inside {DC_Y} -> this.child_id inside {DC_X, SAMP_0, SAMP_1};
```

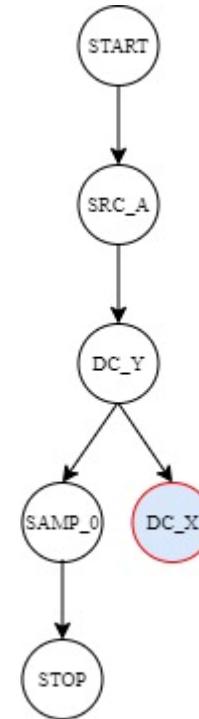


# An Example

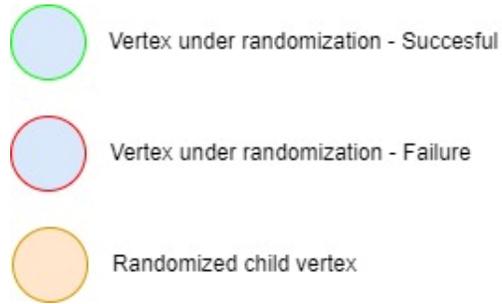
-  Vertex under randomization - Successful
-  Vertex under randomization - Failure
-  Randomized child vertex

```
withdrawn = {SRC_A, DC_Y, SAMP_0, DC_X}
```

```
this.id inside {DC_X} -> this.child_id inside {DC_Y, SAMP_0};
```

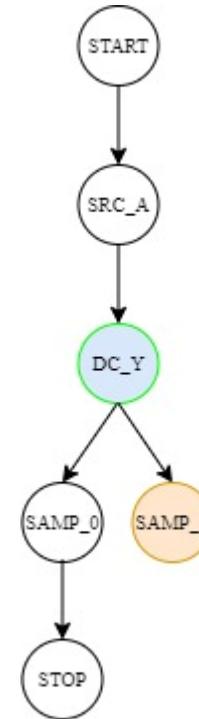


# An Example



```
withdrawn = {SRC_A, DC_Y, SAMP_0, DC_X}
```

```
this.id inside {DC_Y} -> this.child_id inside {DC_X, SAMP_0, SAMP_1};
```

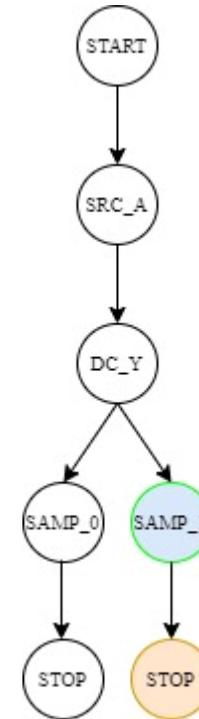


# An Example

-  Vertex under randomization - Successful
-  Vertex under randomization - Failure
-  Randomized child vertex

`withdrawn = {SRC_A, DC_Y, SAMP_0, DC_X, SAMP_1}`

`this.id inside {SAMP_0, SAMP_1, SAMP_2} -> this.child_id inside {STOP};`

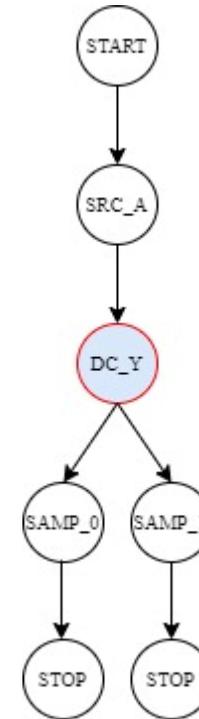


# An Example

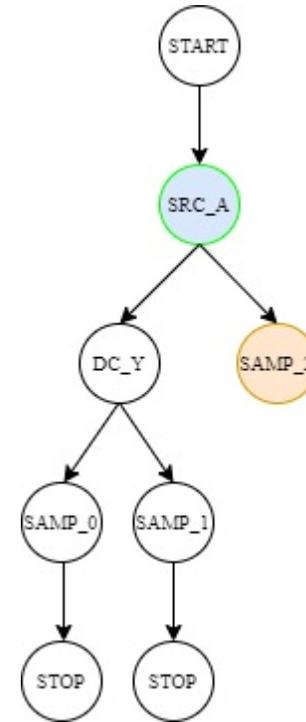
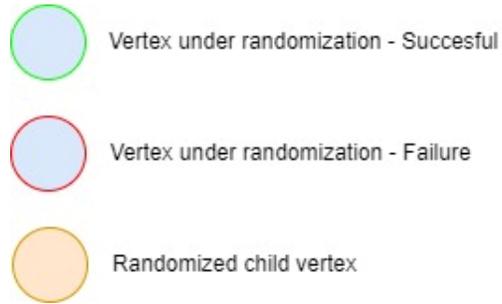
-  Vertex under randomization - Successful
-  Vertex under randomization - Failure
-  Randomized child vertex

```
withdrawn = {SRC_A, DC_Y, SAMP_0, DC_X, SAMP_1}
```

```
this.id inside {DC_Y} -> this.child_id inside {DC_X, SAMP_0, SAMP_1};
```



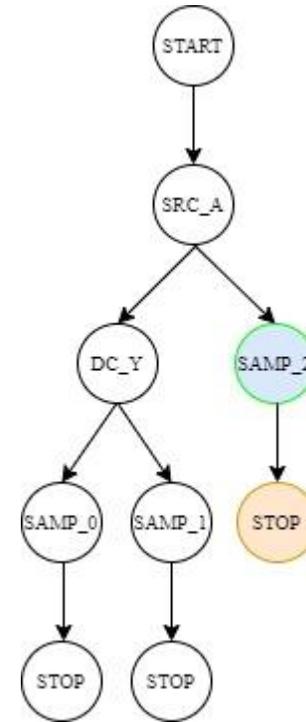
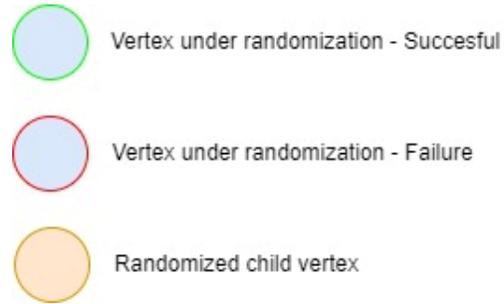
# An Example



`withdrawn = {SRC_A, DC_Y, SAMP_0, DC_X, SAMP_1}`

`this.id inside {SRC_A}      -> this.child_id inside {DC_X, DC_Y, SAMP_0, SAMP_1, SAMP_2};`

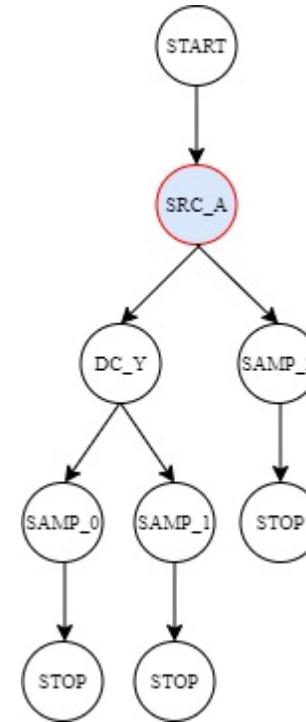
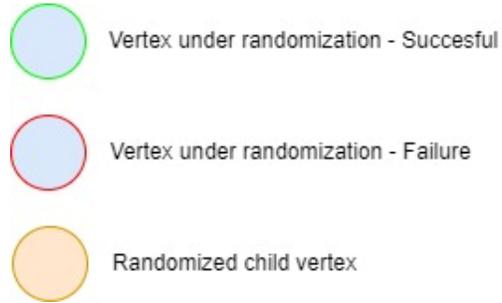
# An Example



`withdrawn = {SRC_A, DC_Y, SAMP_0, DC_X, SAMP_1, SAMP_2}`

`this.id inside {SAMP_0, SAMP_1, SAMP_2} -> this.child_id inside {STOP};`

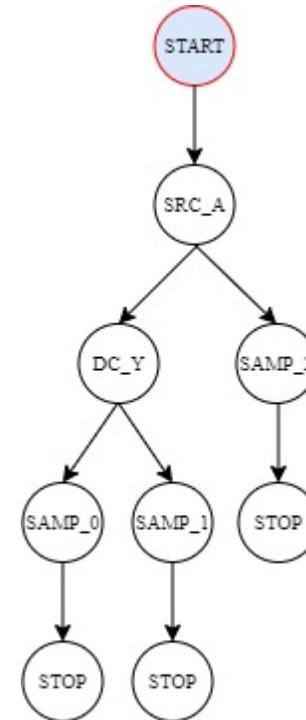
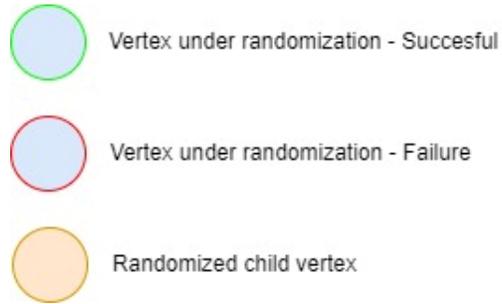
# An Example



withdrawn = {SRC\_A, DC\_Y, SAMP\_0, DC\_X, SAMP\_1, SAMP\_2}

this.id inside {SRC\_A}      -> this.child\_id inside {DC\_X, DC\_Y, SAMP\_0, SAMP\_1, SAMP\_2};

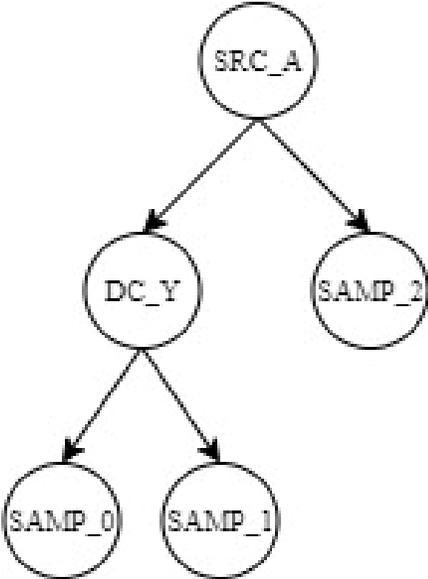
# An Example



withdrawn = {SRC\_A, DC\_Y, SAMP\_0, DC\_X, SAMP\_1, SAMP\_2}

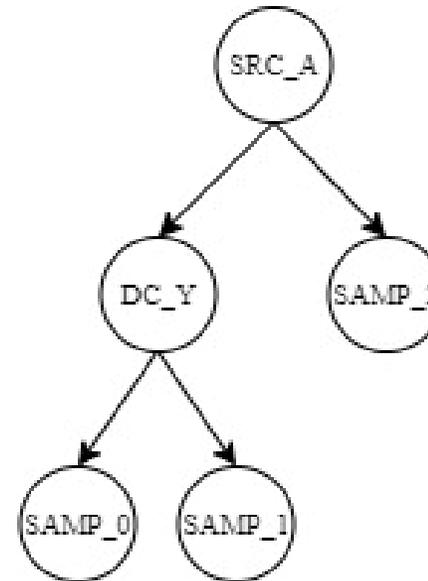
this.id inside {START}      -> this.child\_id inside {SRC\_A, SRC\_B, SRC\_C, SRC\_D};

# A Tree



# Results

- Validity
- Controllability
- Performance
- Scalability



# Results

- Validity
- Controllability
- Performance
- Scalability

```
class sampler0 extends vertex#(id_t, config_t);

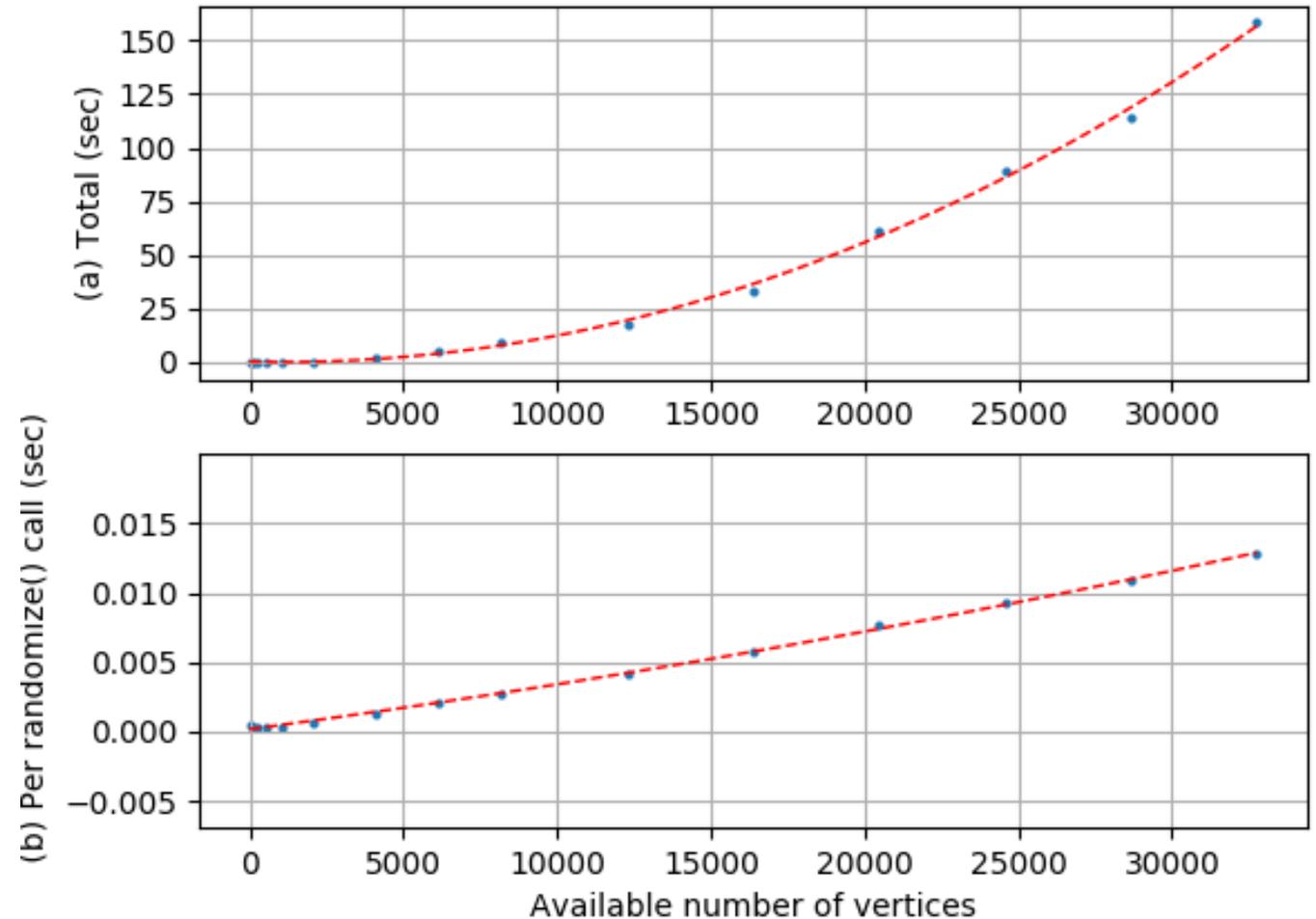
constraint c_samp_0 {
    this.id inside {SRC_A} -> this.child_id inside {DC_X,
                                                    DC_Y,
                                                    SAMP_0};

    this.id inside {DC_X} -> this.child_id inside {SAMP_0};
    this.id inside {DC_Y} -> this.child_id inside {SAMP_0};
    this.id inside {DC_Z} -> this.child_id inside {SAMP_0};
}

...
```

# Results

- Validity
- Controllability
- Performance
- Scalability



# Summary

- Modelling of connectivity
- Recursive, backtracking randomization
- Criteria
- Generic framework



# Q&A

